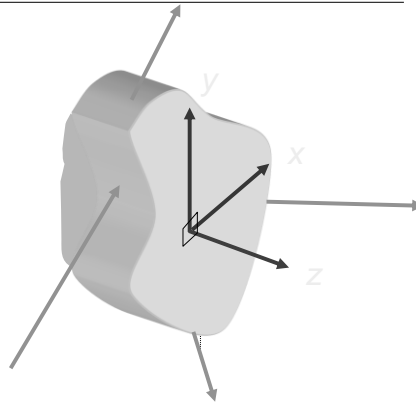


lecture  
two

# loads, forces and vectors



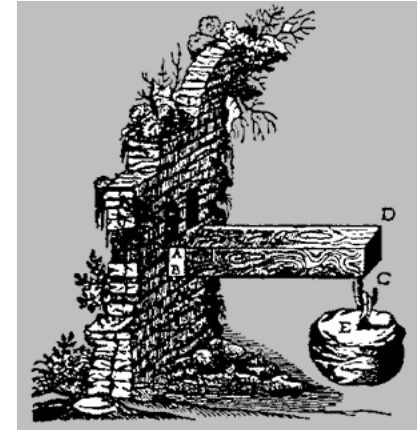
Forces 1  
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## Structural Design

- *planning*
- *preliminary structural configuration*
- *determination of loads*
- *preliminary member selection*
- *analysis*
- *evaluation*
- *design revision*
- *final design*



Forces 5  
Lecture 3

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## Structural Loads

- **STATIC and DYNAMIC**
- **dead load**
  - static, fixed, includes building weight, fixed equipment
- **live load**
  - transient and moving loads (including occupants), snowfall

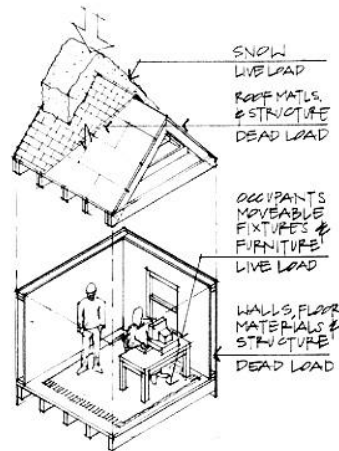


Figure 1.12 Typical building loads.

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## Structural Loads

- **wind loads**
  - dynamic, wind pressures treated as lateral static loads on walls, up or down loads on roofs

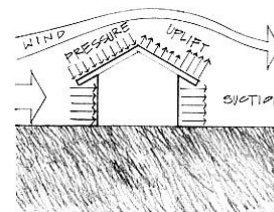
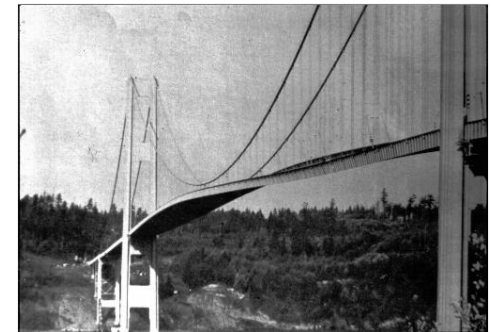


Figure 1.13 Wind loads on a structure.



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## Structural Loads

- **earthquake loads**
  - seismic, movement of ground  $\updownarrow \leftrightarrow$

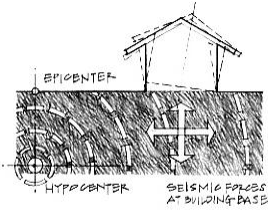
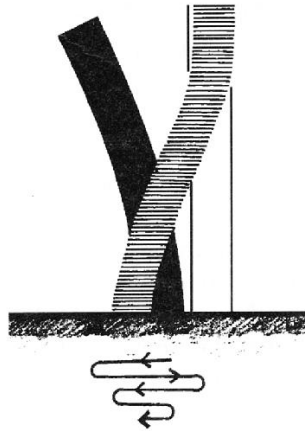


Figure 1.14 Earthquake loads on a structure.



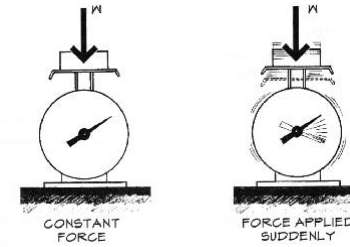
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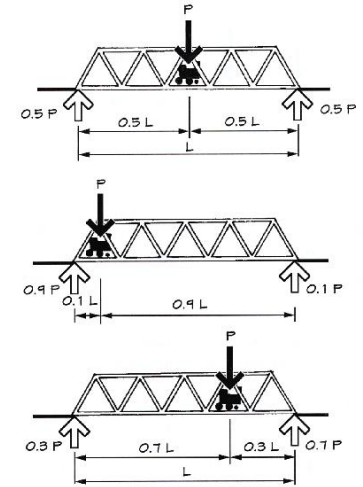
## Structural Loads

- **impact loads**
  - rapid, energy loads



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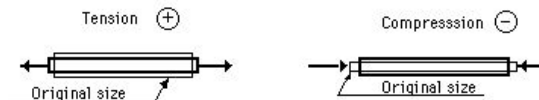


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## Forces

- **statics**
  - physics of forces and reactions on bodies and systems
  - equilibrium (bodies at rest)
- **forces**
  - something that exerts on an object:

- motion
- tension
- compression



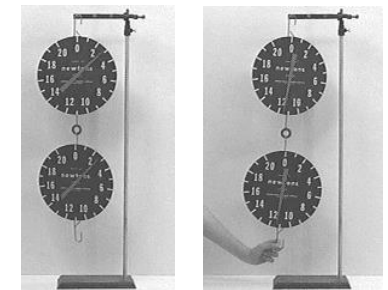
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## Forces

- “action of one body on another that affects the state of motion or rest of the body”
- **Newton’s 3<sup>rd</sup> law:**
  - for every force of action there is an equal and opposite reaction along the same line



<http://nisee.berkeley.edu/godden>

Forces 11  
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## Force Vectors

- applied at a point
- magnitude
  - Imperial units: lb, k (kips)
  - SI units: N (newtons), kN
- direction
- sense



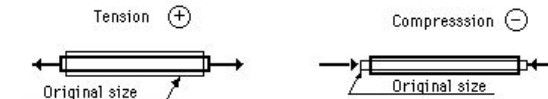
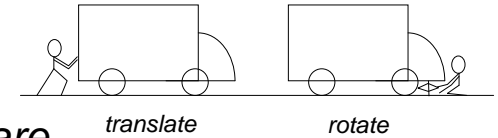
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## Forces on Rigid Bodies

- for statics, the bodies are ideally rigid
- can translate and rotate
- internal forces are
  - in bodies
  - between bodies (connections)
- external forces act on bodies



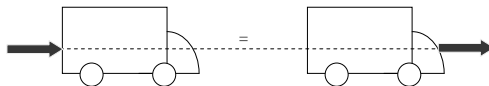
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## Transmissibility

- the force stays on the same line of action
- truck can't tell the difference



- only valid for **EXTERNAL** forces

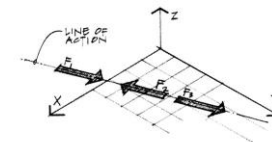
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## Force System Types

- collinear



**Collinear**—All forces acting along the same straight line.  
Figure 2.17(a) Particle or rigid body.

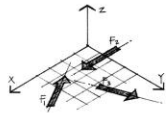
Forces 15  
Lecture 3

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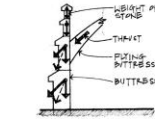
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# Force System Types

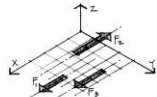
- coplanar



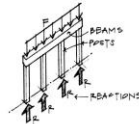
Coplanar—All forces acting in the same plane.  
Figure 2.17(b) Rigid bodies.



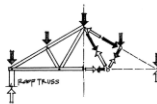
Forces in a buttress system.



Coplanar, parallel—All forces are parallel and act in the same plane.  
Figure 2.17(c) Rigid bodies.



A beam supported by a series of columns.



Loads applied to a roof truss.



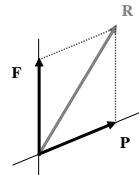
Coplanar, concurrent—All forces intersect at a common point and lie in the same plane.  
Figure 2.17(d) Particle or rigid body.

# Adding Vectors

- graphically

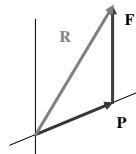
- parallelogram law

- diagonal
- long for 3 or more vectors



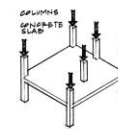
- tip-to-tail

- more convenient with lots of vectors



# Force System Types

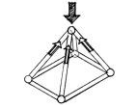
- space



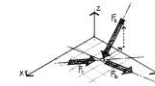
Column loads in a concrete building.



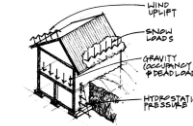
Noncoplanar, parallel—All forces are parallel to each other, but not all lie in the same plane.  
Figure 2.17(e) Rigid bodies.



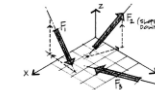
One component of a three-dimensional space frame.



Noncoplanar, concurrent—All forces intersect at a common point but do not all lie in the same plane.  
Figure 2.17(f) Particle or rigid bodies.



Array of forces acting simultaneously on a house.



Noncoplanar, nonconcurrent—All forces are skewed.  
Figure 2.17(g) Rigid bodies.

# Force Components

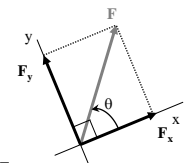
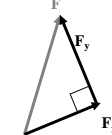
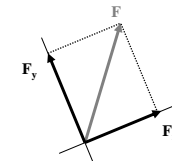
- convenient to resolve into 2 vectors
- at right angles
- in a “nice” coordinate system
- $\theta$  is between  $F_x$  and  $F$  from  $F_x$

$$F_x = F \cos \theta$$

$$F_y = F \sin \theta$$

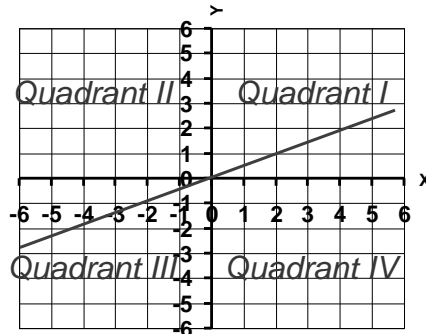
$$F = \sqrt{F_x^2 + F_y^2}$$

$$\tan \theta = \frac{F_y}{F_x}$$



## Trigonometry

- $F_x$  is negative  
– 90° to 270°
- $F_y$  is negative  
– 180° to 360°
- $\tan$  is positive  
– quads I & III
- $\tan$  is negative  
– quads II & IV



Forces 20  
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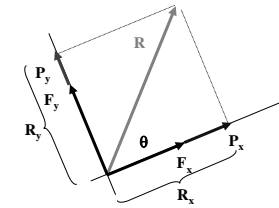
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## Component Addition

- find all x components
- find all y components
- find sum of x components,  $R_x$  (resultant)
- find sum of y components,  $R_y$

$$R = \sqrt{R_x^2 + R_y^2}$$

$$\tan \theta = \frac{R_y}{R_x}$$



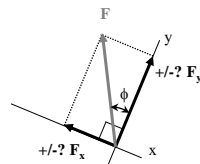
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## Alternative Trig for Components

- doesn't relate angle to axis direction
- $\phi$  is "small" angle between  $F$  and EITHER  $F_x$  or  $F_y$
- no sign out of calculator!
- have to choose **RIGHT** trig function, resulting direction (sign) and component axis



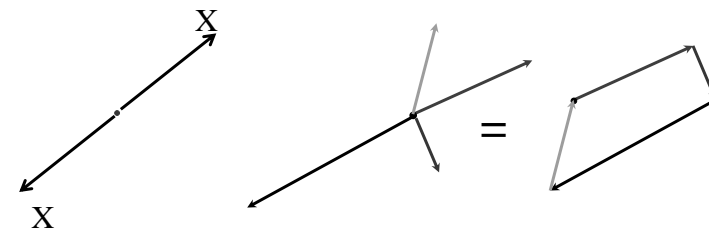
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## Static Equilibrium

- balanced & steady
- no motion or translation
- equilibrant is opposite resultant



Equilibrium 2  
Lecture 5

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## Cables

- simple
- uses
  - suspension bridges
  - roof structures
  - transmission lines
  - guy wires, etc.
- have same tension all along
- can't stand compression



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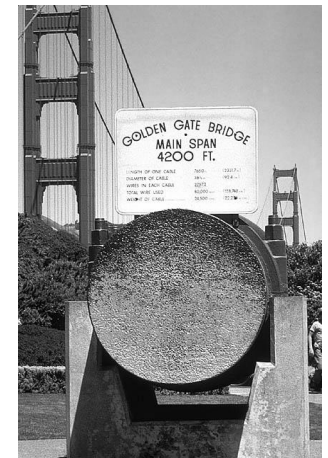
Equilibrium 29  
Lecture 5

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## Cables Structures

- use high-strength steel
- need
  - towers
  - anchors
- don't want movement



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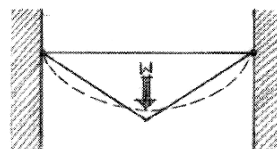
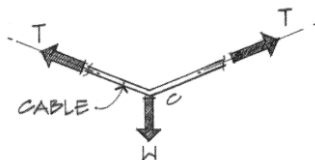
Equilibrium 24  
Lecture 5

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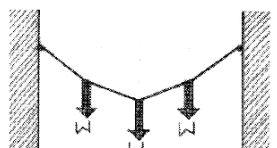
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## Cable Loads

- straight line between forces
- with one force
  - concurrent
  - symmetric



(a) Simple concentrated load—triangle.



(b) Several concentrated loads—polygon.

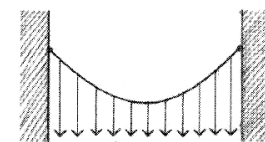
Equilibrium 31  
Lecture 5

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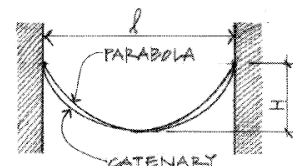
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## Cable Loads

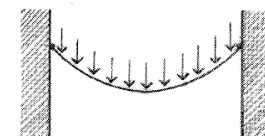
- shape directly related to the distributed load
- funicular



(c) Uniform loads (horizontally)—parabola.



(e) Comparison of a parabolic and a catenary curve.



(d) Uniform loads (along the cable length)—catenary.

Equilibrium 32  
Lecture 5

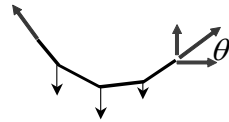
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## Cable Loads

• trig:  $T_x = T \cos \theta$

$$T_y = T \sin \theta$$



• parabolic (catenary)

– distributed uniform load

$$y = 4h(Lx - x^2) / L^2$$

$$L_{total} = L \left( 1 + \frac{8}{3} \frac{h^2}{L^2} - \frac{32}{5} \frac{h^4}{L^4} \right)$$

