

lecture  
twenty five



<http://nisee.berkeley.edu/godden>

# concrete construction: flat spanning systems

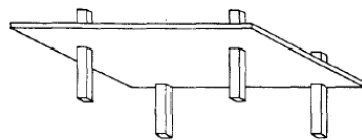
Concrete Spans 1  
Lecture 25

Architectural Structures  
ARCH 331

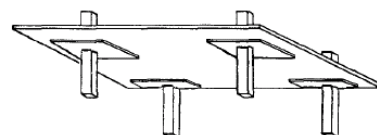
F2009abn

## Reinforced Concrete Design

- flat plate
  - 5”-10” thick
  - simple formwork
  - lower story heights



- flat slab
  - same as plate
  - 2 1/4”-8” drop panels



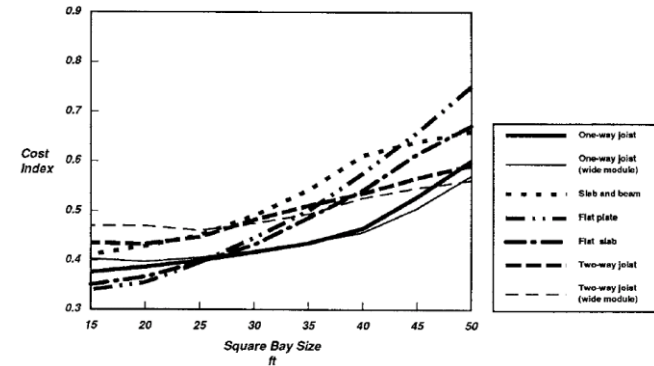
Concrete Spans 3  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

## Reinforced Concrete Design

- economical & common
- resist lateral loads



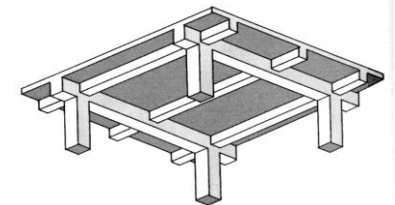
Concrete Spans 2  
Lecture 25

Foundations Structures  
ARCH 331

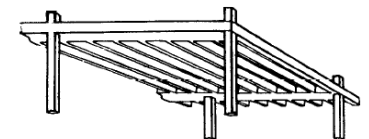
F2008abn

## Reinforced Concrete Design

- beam supported
  - slab depth ~ L/20
  - 8”-60” deep
- one-way joists
  - 3”-5” slab
  - 8”-20” stems
  - 5”-7” webs



The Architect's Studio Companion



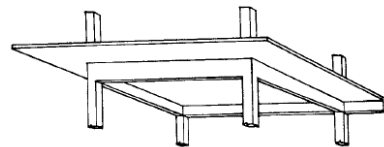
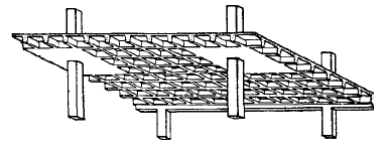
Concrete Spans 4  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

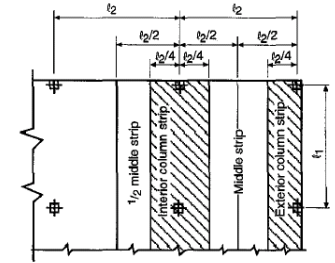
# Reinforced Concrete Design

- two-way joist
  - “waffle slab”
  - 3”-5” slab
  - 8”-24” stems
  - 6”-8” webs
- beam supported slab
  - 5”-10” slabs
  - taller story heights

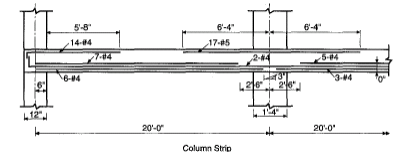


# Reinforced Concrete Design

- simplified frame analysis
  - strips, like continuous beams
- moments require flexural reinforcement
  - top & bottom
  - both directions of slab
  - continuous, bent or discontinuous



(a) Column strip for  $l_2 \leq l_1$



Column Strip

# Reinforced Concrete Design

- one-way slabs (wide beam design)
  - approximate analysis for moment & shear coefficients
  - two or more spans
  - ~ same lengths
  - $w_u$  from combos
  - uniform loads with  $L/D \leq 3$
  - $l_n$  is clear span (+M) or average of adjacent clear spans (-M)

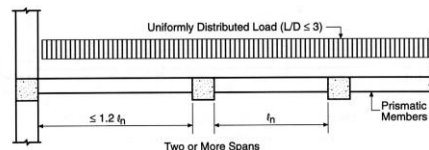


Figure 2-2 Conditions for Analysis by Coefficients (ACI 8.3.3)

# Reinforced Concrete Design

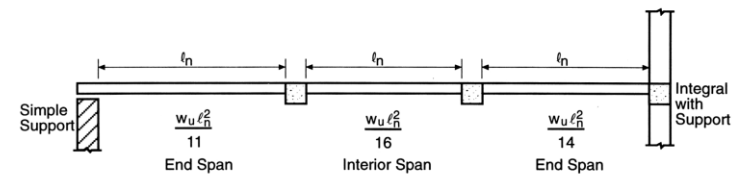


Figure 2-3 Positive Moments—All Cases

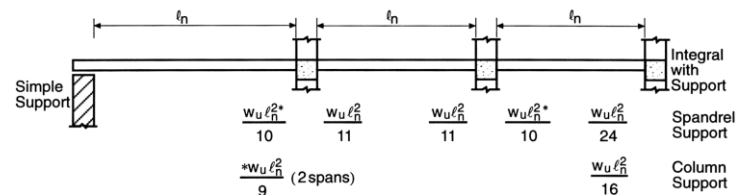
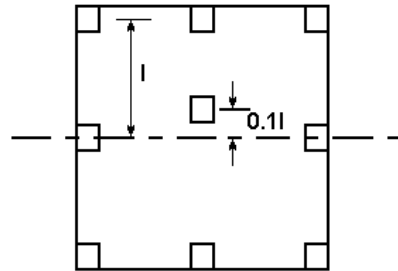


Figure 2-4 Negative Moments—Beams and Slabs

# Reinforced Concrete Design

- *two-way slabs - Direct Design Method*
  - 3 or more spans each way
  - uniform loads with  $L/D \leq 2$
  - rectangular panels with long/short span  $\leq 2$
  - successive spans can't differ  $> longer/3$
  - column offset no more than 10% span



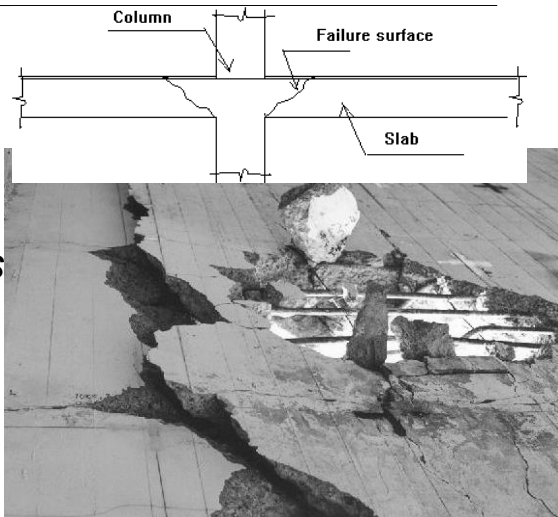
Concrete Spans 9  
Lecture 25

Architectural Structures  
ARCH 331

F2008abn

# Shear in Concrete

- at columns
- want to avoid stirrups
- can use shear studs or heads



Concrete Spans 11  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

# Reinforced Concrete Design

Table 4-6 Two-Way Beam-Supported Slab

Span ratio	Slab Moments	End Span			Interior Span	
		1 Exterior Negative	2 Positive	3 First Interior Negative	4 Positive	5 Interior Negative
0.5	Total Moment	0.16 $M_o$	0.57 $M_o$	0.70 $M_o$	0.35 $M_o$	0.65 $M_o$
	Column Strip Beam	0.12 $M_o$	0.43 $M_o$	0.54 $M_o$	0.27 $M_o$	0.50 $M_o$
	Slab	0.02 $M_o$	0.08 $M_o$	0.09 $M_o$	0.05 $M_o$	0.09 $M_o$
1.0	Middle Strip	0.02 $M_o$	0.06 $M_o$	0.07 $M_o$	0.03 $M_o$	0.06 $M_o$
	Column Strip Beam	0.10 $M_o$	0.37 $M_o$	0.45 $M_o$	0.22 $M_o$	0.42 $M_o$
	Slab	0.02 $M_o$	0.06 $M_o$	0.08 $M_o$	0.04 $M_o$	0.07 $M_o$
2.0	Middle Strip	0.04 $M_o$	0.14 $M_o$	0.17 $M_o$	0.09 $M_o$	0.16 $M_o$
	Column Strip Beam	0.06 $M_o$	0.22 $M_o$	0.27 $M_o$	0.14 $M_o$	0.25 $M_o$
	Slab	0.01 $M_o$	0.04 $M_o$	0.05 $M_o$	0.02 $M_o$	0.04 $M_o$
	Middle Strip	0.09 $M_o$	0.31 $M_o$	0.38 $M_o$	0.19 $M_o$	0.36 $M_o$

- Notes: (1) Beams and slab satisfy stiffness criteria:  $\alpha_1 l_2 / b_1 \geq 1.0$  and  $\beta_1 \geq 2.5$ .  
 (2) Interpolate between values shown for different  $l_2 / l_1$  ratios.  
 (3) All negative moments are at face of support.  
 (4) Concentrated loads applied directly to beams must be accounted for separately.

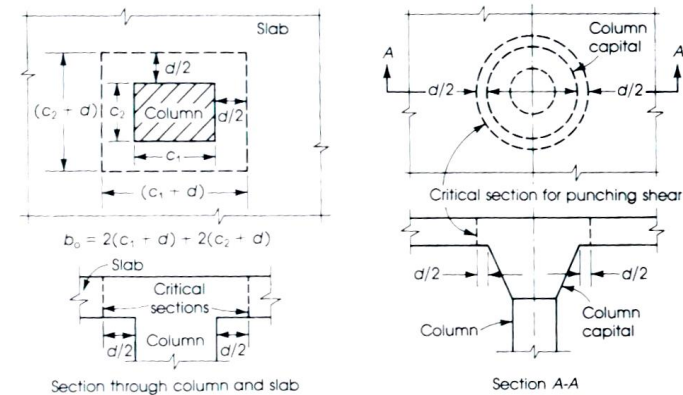
Concrete Spans 10  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

# Shear in Concrete

- critical section at  $d/2$  from
  - column face, column capital or drop panel



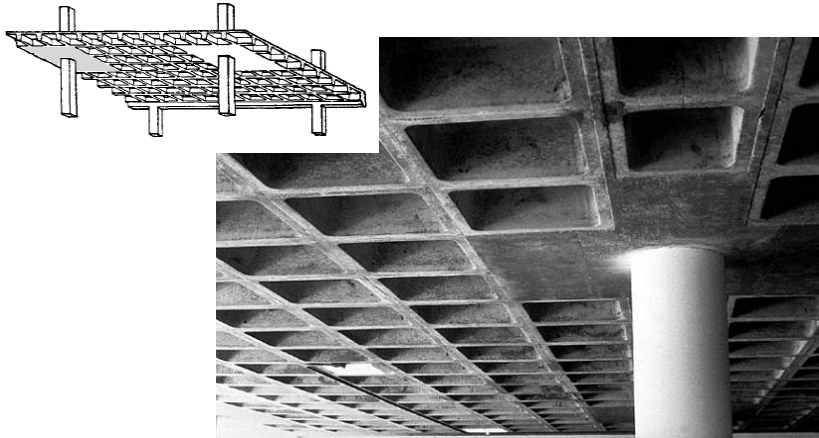
Concrete Spans 12  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

## Shear in Concrete

- at columns with waffle slabs



Concrete Spans 13  
Lecture 25

Foundations Structures ARCH 331 <http://nisee.berkeley.edu/godden> F2008abn

## General Beam Design

- $f'_c$  &  $f_y$  needed
- usually size just  $b$  &  $h$ 
  - even inches typical (forms)
  - similar joist to beam depth
  - $b:h$  of 1:1.5-1:2.5
  - $b_w$  &  $b_f$  for  $T$
  - to fit reinforcement + stirrups
- slab design,  $t$ 
  - deflection control & shear

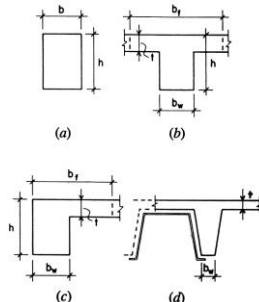


Figure 14.5 Common shapes for beams.

$$S = \frac{bh^2}{6}$$

Concrete Spans 15  
Lecture 25

Foundations Structures ARCH 331

F2008abn

## Openings in Slabs

- careful placement of holes
- shear strength reduced
- bending & deflection can increase

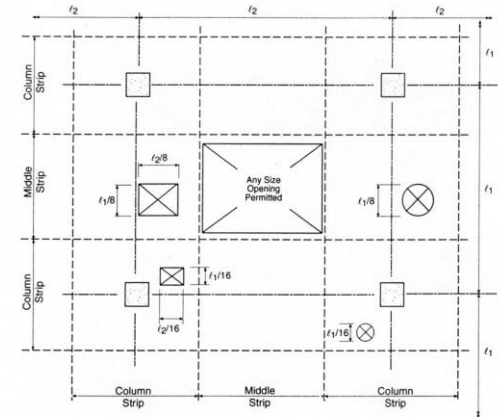


Figure 18-11 Openings in Slab Systems without Beams

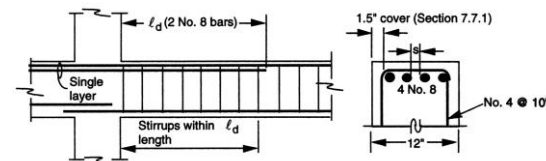
Concrete Spans 14  
Lecture 25

Foundations Structures ARCH 331

F2008abn

## General Beam Design (cont'd)

- custom design:
  - longitudinal steel
  - shear reinforcement
  - detailing



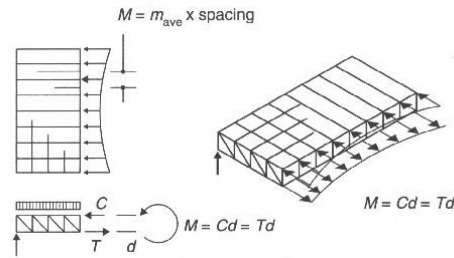
Concrete Spans 16  
Lecture 25

Foundations Structures ARCH 331

F2008abn

## Space "Frame" Behavior

- handle uniformly distributed loads well
- bending moment
  - tension & compression "couple" with depth
  - member sizes can vary, but difficult



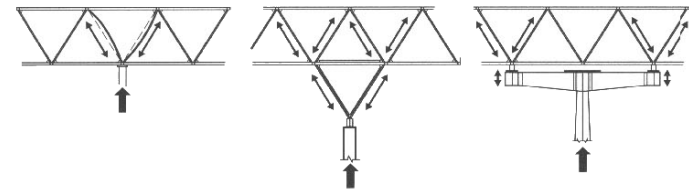
Concrete Spans 17  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

## Space "Frame" Behavior

- shear at columns
- support conditions still important
  - point supports not optimal
- fabrication/construction can dominate design



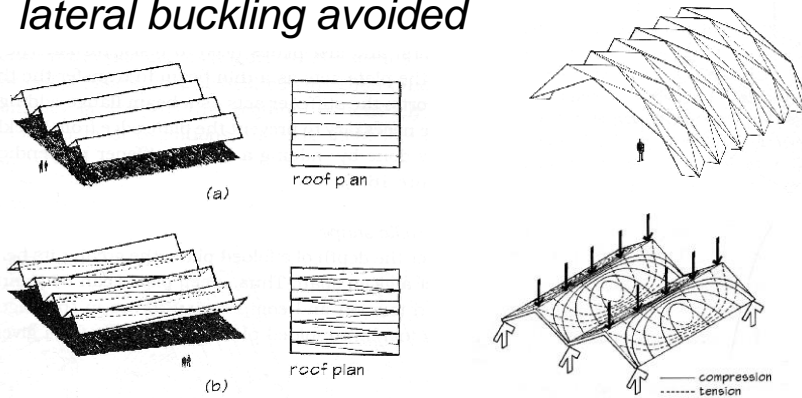
Concrete Spans 18  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

## Folded Plates

- increased bending stiffness with folding
- lateral buckling avoided



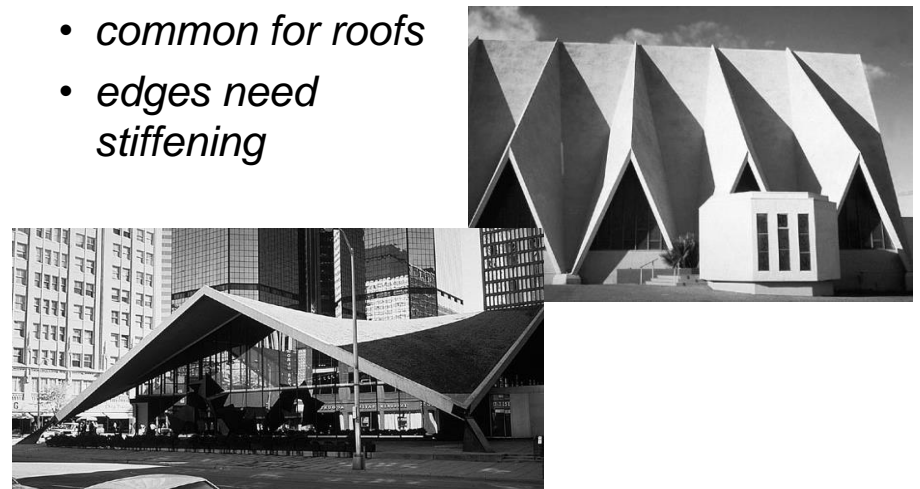
Concrete Spans 19  
Lecture 25

Foundations Structures  
ARCH 331

F2008abn

## Folded Plates

- common for roofs
- edges need stiffening



<http://nisee.berkeley.edu/godden>

Concrete Spans 20  
Lecture 25

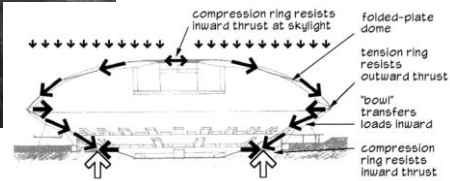
Foundations Structures  
ARCH 331

F2008abn

# Folded Plates



www.library.illinois.edu



- *State Farm Center (Assembly Hall), University of Illinois*
- *Harrison & Abramovitz 1963*
- *Edge-supported dome spanning 400 feet woud with 614 miles of one-fifth inch steel wire*